Problem of the Month - March 2024

In a dance competition with n dancers (where $n > 2$), each dancer performed exactly once. For every pair of dancers, there was a moment when both were dancing simultaneously. Prove that, at some point, all the dancers were dancing simultaneously.